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SEQUAN: A COMPUTER PROGRAM FOR SEQUENTIAL ANALYSIS

Abstract.—A description of a FORTRAN IV computer program for performing sequential analysis on four common distributions after the underlying probability distribution is known.

Decision-making and cost-reduction are key concepts in management research. Sequential hypothesis-testing procedures that were developed for quality control in industrial processes (2, 3, 5) have been applied in a limited way to biological problems. Forest entomologists have used the sequential probability ratio test of Sobel and Wald (2) to classify insect populations (4) and to evaluate the need for insect control (1). This note describes briefly a computer program that was developed to eliminate much of the computational work associated with sequential analysis.

Sequential analysis is popular with forest entomologists because, on the average, it requires fewer observations for fixed type-1 (α) and type-2 (β) errors than fixed-sample size plans require. The smaller the difference to be detected at a given type-1 (α) and type-2 (β) error, the larger the average sample size. In this method of analysis we assume that the observations are independent and the probability distribution is known beforehand.

To perform any sequential analysis, the following must be known:

1. A description of the underlying probability distribution.
2. A statement of the hypothesis that is to be tested.
3. The type-1 (α) and type-2 (β) errors.

The computer program was developed for the three-decision problem (light, medium, heavy) that is commonly encountered by forest entomologists. By repeating selected input data in certain columns of the

second control card, the program can be used to obtain the required statistics for the two-decision problem (control *vs* no control).

The FORTRAN IV program was developed by the authors on a 7094 computer. The program will provide the following statistics for the binomial, negative binomial, poisson, and normal distributions:

1. Equations for the decision lines.
2. Table of decision boundaries.
3. Graph of decision lines.
4. List of selected points for the operating-characteristics (OC) curve.
5. List of selected points for the average-sample-number (ASN) curve.

For the normal and negative binomial distributions, it is assumed that the variance and k-value are known beforehand.

Description of Control Deck

The user must supply the following control cards when using the program. Two control cards are required for each analysis desired. The first control card contains the type-1 (α) and type-2 (β) errors, the distribution index, and the number of decision points to be printed.

Card 1	Column	Format	
	1 - 3	F3.2	Type-1 error, A
	4 - 6	F3.2	Type-2 error, B
	7 - 8	I2	Distribution index
	9 - 11		01 - Binomial 02 - Negative binomial 03 - Poisson 04 - Normal I3 Number of decision points to be printed

The second control card contains the parameters needed for the analysis. The format of this control card depends upon the distribution. Binomial distribution:

$$H_0: P < P_1$$

$$H_1: P_2 \leq P \leq P_3$$

$$H_2: P > P_3$$

Column	Format	Description
1 - 8	F8.4	P_1
9 - 16	F8.4	P_2
17 - 24	F8.4	P_3
25 - 32	F8.4	P_4

Negative binomial:

$$H_0: M < M_1$$

$$H_1: M_2 \leq M \leq M_3$$

$$H_2: M > M_4$$

<i>Column</i>	<i>Format</i>	<i>Description</i>
1 - 8	F8.4	M_1
9 - 16	F8.4	M_2
17 - 24	F8.4	M_3
25 - 32	F8.4	M_4
33 - 40	F8.4	K - "Index of aggregation"

Poisson:

$$H_0: \lambda < \lambda_1$$

$$H_1: \lambda_2 \leq \lambda \leq \lambda_3$$

$$H_2: \lambda > \lambda_4$$

<i>Column</i>	<i>Format</i>	<i>Description</i>
1 - 8	F8.4	λ_1
9 - 16	F8.4	λ_2
17 - 24	F8.4	λ_3
25 - 32	F8.4	λ_4

Normal:

$$H_0: \mu < \mu_1$$

$$H_1: \mu_2 \leq \mu \leq \mu_3$$

$$H_2: \mu > \mu_4$$

<i>Column</i>	<i>Format</i>	<i>Description</i>
1 - 8	F8.4	μ_1
9 - 16	F8.4	μ_2
17 - 24	F8.4	μ_3
25 - 32	F8.4	μ_4
33 - 42	F10.4	σ - standard deviation

Example

Suppose we wish to calculate the sequential plan described by Waters (4) for the spruce budworm. The basic data for this plan were fitted to the negative binomial distribution. Waters listed the following parameters for his plan:

$$\begin{aligned} \alpha &= 0.10 \\ M_1 &= 3.00 \\ M_3 &= 9.00 \end{aligned}$$

$$\begin{aligned} \beta &= 0.10 \\ M_2 &= 6.00 \\ M_4 &= 12.00 \end{aligned}$$

$$k = 7.288$$

Figure 1.—Program output of decision equations and sequential table.

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      SEQUAN      ALPHA = 0.100      BETA = 0.100
      NEG BIN    P1 = 0.415     P2 = 0.830     P3 = 1.245     P4 = 1.660     K = 7.228
      CASE 1      PO VS PI      PO .GT. PI      LOW VS MEDIUM
      LOWER = -5.040+   4.265 N
      UPPER =  5.040+   4.265 N
      CASE 2      PO VS P2      P2 .GT. PO      MEDIUM VS HIGH
      LOWER = -18.612+ 10.386 N
      UPPER = 1E.612+ 10.386 N
      LOWER      MEDIUM      UPPER
      N          LOW VS MEDIUM      MEDIUM VS HIGH
      LOW        HIGH           LOW      HIGH
      1          -0       9           -7      29
      2          3        14          2       39
      3          8        18          13      50
      4          12       22          23      60
      5          16       26          33      71
      6          21       31          44      81
      7          25       35          54      91
      8          29       39          64      102
      9          33       43          75      112
      10         38       48          85      122
      11         42       52          96      133
      12         46       56          106     143
      13         50       60          116     154
      14         55       65          127     164
      15         59       69          137     174
      16         63       73          148     185
      17         67       78          158     195
      18         72       82          168     206
      19         76       86          179     216
      20         80       90          189     226
      21         85       95          199     237
      22         89       99          210     247
      23         93      103          220     257
      24         97      107          231     266
      25        102      112          241     276
  
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Figure 2.—Graph of decision line equations.

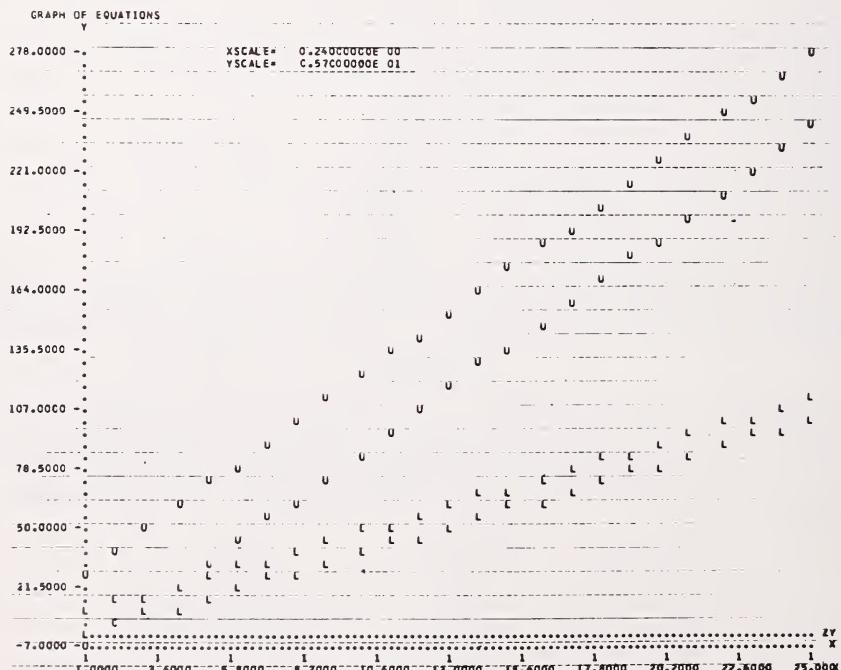


TABLE OF VALUES FOR THE OC AND ASN CURVES-- NEG BIN

CASE 1			CASE 2		
LOW	VS MEDIUM	MEDIUM VS HIGH	LOW	VS MEDIUM	ASA
P	OC	ASN	P	OC	ASA
0.595	0.486	3.730	1.432	0.514	13.767
0.600	0.473	3.713	1.427	0.527	13.726
0.606	0.459	3.694	1.421	0.541	13.734
0.611	0.445	3.673	1.416	0.555	13.736
0.621	0.418	3.626	1.406	0.582	13.720
0.632	0.392	3.572	1.396	0.608	13.678
0.643	0.366	3.513	1.386	0.634	13.609
0.654	0.341	3.448	1.376	0.659	13.516
0.666	0.317	3.379	1.366	0.683	13.401
0.677	0.293	3.305	1.357	0.707	13.265
0.701	0.250	3.149	1.337	0.750	12.939
0.725	0.211	2.984	1.318	0.789	12.554
0.750	0.177	2.815	1.300	0.823	12.128
0.776	0.147	2.647	1.281	0.853	11.675
0.803	0.122	2.482	1.263	0.878	11.210
0.830	0.100	2.323	1.245	0.900	10.744
1.156	0.012	1.202	1.080	0.988	7.046
2.179	0.000	0.439	0.816	1.000	4.148
MEAN 1 =	3.0000	CC-VALUE = 0.900	MEAN 2 =	6.0000	CC-VALUE = 0.100
MEAN 3 =	9.0000	CC-VALUE = 0.900	MEAN 4 =	12.0000	CC-VALUE = 0.100

Figure 3.—Program output of OC and ASN values.

From this information the control deck would be prepared as follows:

COLUMN NO

Card

Card	No.	1	2	3	4	5	6	7	8	9 ¹	0	1	2	3	4	5	6	7	8	9 ²	0	1	2	3	4	5	6	7	8	9 ³	0	1	2	3	4	5	6	7	8	9 ⁴	0
1		0	1	0	0	1	0	0	2	0	2	5																													
2		0	0	0	3	0	0	0	0	0	0	0	0	6	0	0	0	0	0	0	0	9	0	0	0	0	0	0	1	2	0	0	0	0	0	7	2	2	8	0	

Figures 1, 2, and 3 show the sequential plan produced by this program. The decision-line equations produced by this program differ slightly from those published by Waters, but these differences are probably due to rounding errors. The occasional discrepancies between values in the sequential tables are also the results of rounding errors.

A program deck with examples can be obtained from the authors.

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